SPSC: AN EFFICIENT, GENERAL-PURPOSE EXECUTION POLICY FOR STOCHASTIC SIMULATIONS

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ABSTRACT
In this paper, we present a stochastic simulation execution policy named SPSC from its different steps: Simulation, Partitioning, Selection, Cloning. It does not require prior knowledge on the model to be applied and allows one to estimate efficiently the probabilities of possible simulation outcomes, so called solutions. It is evaluated on three different multi-agent-based simulations. Results show that SPSC could be a relevant alternative to the Monte Carlo method.

1 INTRODUCTION
Stochastic simulations are widely used in application domains where no deterministic laws can be used to predict the future state of the system. The results of such simulations being variable by nature, it is mandatory to replicate their execution in order to retrieve experimentally the distribution of possible simulation outcomes, so called solutions and then obtain their probabilities. In the general case, the Monte-Carlo (MC) method is classically used (Rubinstein and Kroese 2016). Nevertheless, if computing resources are limited or solutions of interest are rare, MC can be inefficient (Rubino et al. 2009).

In this paper, we present a simulation execution policy called SPSC, based on the clustering, selection and cloning of replication states, in order to improve the quality of the results for a fixed computing cost while being as generic as possible. The general idea of this policy is to constrain the evolution of the replications by periodically selecting and cloning those potentially leading to interesting results for the decision maker. These ideas were shortly introduced in Huang et al. (2019). Here, we extend that original presentation, with refined analyses and experiments.

After formalizing the problem, we present some existing solutions in Section 2. Our approach, as well as its implementation are detailed in Section 3. Finally, the policy is validated on two academic agent-based models (prey-predator and virus transmission), then on a more complex traffic simulation. Experiments and results are discussed in Section 4. Finally, we conclude by presenting the main perspectives of this work.

2 PREAMBLE
2.1 Problem formalization
The state of a stochastic simulation is fully characterized by the set of its state variables. Nevertheless, it can be very large. Thus, to be interpreted by a decision maker, this raw state is generally reduced to a set of meaningful observables that sums it up, e.g., for a population of individuals, the observables could be its size, the mean age of the individuals, the sex-ratio, etc.
Observables at time step $t$ can be represented by a random vector $X_t$. We denote $\mathcal{D}$ the domain of vector $X_t$. Decision makers are often interested by some sets of specific values that the vector $X_t$ can take. Such a set $\mathcal{S}$ is called a solution which is by nature a subset of domain $\mathcal{D}$, i.e., $\mathcal{S} \subseteq \mathcal{D}$.

The main goals of a stochastic simulation are to determine if a solution $\mathcal{S}$ is possible and its probability $\mathbb{P}(X_t \in \mathcal{S}) = \theta_\mathcal{S}$ at time step $t$ (in general the last time step). In the general case, obtaining an analytical expression of the distribution of $X_t$ is virtually impossible. Hence the study of such a solution consists in building an estimator $\hat{\theta}_\mathcal{S}$ of $\theta_\mathcal{S}$ over a set of replications executed according to a specific policy.

### 2.2 Monte Carlo simulation

The Monte Carlo method (MC) is a classical execution policy to address this problem. It consists in simulating a number $n$ of replications (i.e., obtaining $n$ independent and identically distributed samples) and building an estimator (generally the Maximum likelihood estimator) $\hat{\theta}_\mathcal{S}$ of $\theta_\mathcal{S}$ defined as:

$$\hat{\theta}_\mathcal{S} = \frac{1}{n} \sum_{i=1}^{n} 1_{\mathcal{S}}(X_t^i)$$

where $1_{\mathcal{S}}$ is the indicator function of solution $\mathcal{S}$ and $X_t^i$ the value of observables in the $i$th replication (Rubinstein and Kroese 2016). Of course, the number $n$ has to be large enough for the estimator to be good. The minimal number of replications to obtain a good estimator $\hat{\theta}_\mathcal{S}$ of the probability $\mathbb{P}(X_t \in \mathcal{S}) = \theta_\mathcal{S}$ of some solution $\mathcal{S}_i$ where $X_t^i$ is one observable of the vector $X_t$ is denoted $n(X_t^i)$. Suppose a desired relative error $\varepsilon$ for the estimator $\hat{\theta}_\mathcal{S}$ at confidence level $1 - \alpha$:

$$\mathbb{P}\left(\left|\frac{\hat{\theta}_\mathcal{S} - \theta_\mathcal{S}}{\theta_\mathcal{S}}\right| \leq \varepsilon \right) \geq 1 - \alpha.$$  

The minimal value for $n(X_t^i)$ to verify (2) can be approximated by applying the following algorithm (Banks et al. 2010):

1. Simulate $n_0$ replications. ($n_0$ observations $X_t^{i_1}, \ldots, X_t^{i_{n_0}}$)
2. Compute

$$n(X_t^i) = \lceil \left( \frac{Z_{1-(\alpha/2)}}{\varepsilon \cdot \overline{X}_{t^i}} \right)^2 \rceil$$

where $Z_{1-(\alpha/2)}$ is the $100(1 - \alpha/2)$ quantile of the normal distribution, $\mathcal{S}_i$ stands for the sample standard deviation over the $n_0$ observations and $\overline{X}_{t^i}$ is the sample mean value over the $n_0$ observations. The conventional values for $n_0$, $\varepsilon$ and $\alpha$ are respectively 150, 0.05 and 0.05.

### 2.3 Related execution policies

Other execution policies have been proposed to be used in specific contexts. The most relevant are briefly presented in the following.

If simulations rely on a Markov model and the solution of interest is unique and rare, methods such as splitting or importance sampling can be used.

The idea behind the Splitting methods consists in decomposing the target rare solution $\mathcal{S}$ into an event chain $E_0, \ldots, E_n$, which satisfies $\mathcal{S} = E_n \subset E_{n-1} \subset \ldots \subset E_0$. Initially, $N$ replications from $t_0$ to $t$ are simulated. Then, those reaching the event $E_0$ at time $t_0 < t$ are cloned. Afterward, these cloned replications are simulated from $t_l$ to $t$ and those reaching $E_1$ are cloned once again. The process is repeated until $E_n = \mathcal{S}$ is reached (Villén-Altamirano and Villén-Altamirano 1994; L’Ecuyer et al. 2009). Finally, $\hat{\theta}_\mathcal{S}$ is computed from the product of conditional probabilities:

$$\hat{\theta}_\mathcal{S} = P(E_0) \prod_{i=1}^{n} P(E_{i+1}|E_i).$$
Importance Sampling (IS) relies on the substitution of the distribution of random variables. The basic idea is to obtain samples generated from a different distribution leading more often to the solution of interest (Glynn and Iglehart 1989). The probability estimation over these samples is biased, however it is possible to reconstruct an unbiased estimator combining the biased one and the relation between the two distributions.

The polyagent approach has been introduced by Parunak et al. to quickly characterize the mean trajectory of a stochastic multi-agent-based simulation (Parunak and Brueckner 2006). Periodically, agents generate a set of *ghosts*, i.e., virtual agents that mimic their behavior and mark the explored trajectories with pheromones. Then, the agent goes up the gradient of the calculated pheromone field until it reaches its maximum, which defines its new state.

The idea behind *simulation cloning* is that if different replications generate the same trajectory, then, it is more efficient to simulate one replication and clone it at decision points, i.e., when processing a non-deterministic event, to explore alternative futures (Hybinette and Fujimoto 1997; Hybinette and Fujimoto 2001). This approach allows one to perform "what-if" scenarios, e.g., to determine the consequences of different scheduling algorithms in manufacturing simulations.

The policies presented in this section can be powerful and efficient, but being specific to a modeling paradigm or a particular problem, it is not straightforward to apply them in the general case. For instance, although splitting seems simple, we need to know the chain of events leading to the target solution. IS relies on Markov models and requires not only a full knowledge of the random variable distribution to skew but also low-level access to the pseudo-random number generator. The polyagent approach can only be applied on multiagent-based simulations and target one solution: the most probable. In the simulation cloning approach, decisions points must be known and their number should be limited to prevent combinatorial explosion.

3 SPSC: A GENERAL-PURPOSE EXECUTION POLICY

The proposed execution policy has been named according to the successive steps of the process: Simulation, Partitioning, Selection and Cloning.

3.1 General principle

Instead of executing the replications from $t_0$ to $t_f$ as MC does, the temporal interval $[t_0,t_f]$ is cut into $m$ sub-intervals $[t_{(i)},t_{(i+1)}]$, $i = 0,\ldots,m-1$, such as:

$$[t_0,t_f] = \bigcup_{i=0}^{m-1} [t_{(i)},t_{(i+1)}]$$

(5)

and

$$[t_{(i)},t_{(i+1)}] \cap [t_{(j)},t_{(j+1)}] = \left\{ \begin{array}{ll} t_{(i+1)} & \text{if } j = i + 1, \\ \emptyset & \text{if } j = i, \\ t_{(i)},t_{(i+1)} & \text{else,} \end{array} \right.$$  

(6)

with $t_{(0)} = t_0$ and $t_{(m)} = t_f$.

Then, for each sub-interval $[t_{(i)},t_{(i+1)}]$, the following steps, illustrated by Figure 1, are applied:

**Simulation:** Execute $N$ replications from $t_{(i)}$ to $t_{(i+1)}$.

**Partitioning:** At time step $t_{(i+1)}$, retrieve the observables from the states of each replication then partition these $N$ states into $K$ subsets according to these observables.

**Selection:** Select one or more representative replications in each subset. Then, delete the non selected replications.
Cloning: Clone the selected replications to reach $N$ replications in total (to control the computational cost).

Once the replications reach the final time step $t_f$, the results can be analyzed to obtain an estimation of the probability of the solutions.

3.2 Estimation of the probability of solutions

As shown in Section 2.1, our main goals are the detection of possible solutions at final time step $t_f$ and the estimation of their probabilities. We recall here some notations: the observables of a replication at $t$, the observables of a replication at $t_f$ are represented by a random vector $X_{t_f}$, the interesting solution is denoted $\mathcal{S}$, its probability $P(X_{t_f} \in \mathcal{S})$ and the probability estimator $\hat{\theta}_\mathcal{S}$.

Contrary to MC, the Maximum likelihood estimator cannot be applied to SPSC. Indeed, some replications are removed during the simulation and replaced by clones. Thus, we introduce an estimator suitable in our case, based on the decomposition of the target probability and its reconstruction.

Decomposition of the probability of interest

The theoretical probability $P(X_{t_f} \in \mathcal{S})$ can be decomposed using the law of total probability. Considering an intermediate time step $j$, we can rewrite this probability as:

$$P(X_{t_f} \in \mathcal{S}) = \sum_{\mathcal{S}_j \in \mathcal{P}_j} P(X_{t_f} \in \mathcal{S} | X_j \in \mathcal{S}_j) P(X_j \in \mathcal{S}_j)$$

(7)

where $\mathcal{P}_j$ is a partition of the state variable space $X_j$.

More generally, by assuming that the studied system has the Markov property, i.e., $X_i$ depends only on $X_{i-1}$, the decomposition can then be extended:

$$P(X_{t_f} \in \mathcal{S}) = \sum_{\mathcal{S}_{m-1} \in \mathcal{P}_{m-1}} \prod_{i=0}^{m-1} P(X_{t_i+1} \in \mathcal{S}_{i+1} | X_i \in \mathcal{S}_i)$$

(8)

where $\mathcal{P}_i$, $i=1,...,m-1$ is the partition of the state variable space $X_i$, $\mathcal{S}_T = \mathcal{S}$ and $\mathcal{S}_0$ are the initial states of the simulation.

Reconstitution of probability estimators

In this Section, we present a method allowing to compute the estimator of $P(X_{t_f} \in \mathcal{S})$ inspired by the probability decomposition presented in Equation (8).

Once SPSC iterations are over, we have for each intermediate time step $t(i)$ a partition $\mathcal{P}(i)$ for the state variable space $X_{t(i)}$. For an element $\mathcal{S}(i)$ of the partition $\mathcal{P}(i)$, after the selection and cloning steps, $n_i$ replications have then been cloned. From these $n_i$ cloned replications, some $(n_{i+1})$ will be associated to an element $\mathcal{S}_{i+1} \in \mathcal{P}(i+1)$ after the partitioning step at time step $t(i+1)$. The quantities $n_i$ and $n_{i+1}$ can then be used to estimate the conditional probability $P(X_{t(i+1)} \in \mathcal{S}_{i+1} | X_{t(i)} \in \mathcal{S}(i))$ by:

$$\hat{P}(X_{t(i+1)} \in \mathcal{S}_{i+1} | X_{t(i)} \in \mathcal{S}(i)) = \frac{n_{i+1}}{n_i}$$

(9)

Eventually, we can define a new estimator $\hat{\theta}_\mathcal{S}$ for $P(X_{t_f} \in \mathcal{S})$ from Equation (9), using a decomposition similar to Equation (8):

$$\hat{\theta}_\mathcal{S} = \sum_{\mathcal{S}_{m-1} \in \mathcal{P}_{m-1}} \prod_{i=0}^{m-1} \hat{P}(X_{t(i+1)} \in \mathcal{S}_{i+1} | X_{t(i)} \in \mathcal{S}(i))$$

(10)
where \( \mathcal{I}(m) = \mathcal{I} \) and \( \mathcal{I}(0) = \mathcal{I}_0 \).
1. Identify the solutions of interest.
2. Estimate the reference probability value (as we do not have analytical solutions).
3. Run simulation batches using MC and SPSC with the same amount of resources.
4. Statistically compare the results according to the metrics presented in Section 4.1

4.1 Policies evaluations and comparisons

To evaluate a stochastic simulation execution policy and its associated probability estimator, two performance measures can be computed from a batch of replications: the detection capabilities of the policy, i.e., its ability to reach a possible solution and the precision of its probability estimator.

Detection   To evaluate the detection capabilities of an execution policy for a specific solution $S$, the following indicator function is used:

$$Detect(S) = \begin{cases} 
1 & \text{if one of the replication reaches } S \\
0 & \text{else.} 
\end{cases}$$  
(11)

For a set of solutions $S$, we measure the detection of all the solutions simultaneously:

$$Detect(S) = \begin{cases} 
1 & \text{if } \forall S \in S, Detect(S) = 1 \\
0 & \text{else.} 
\end{cases}$$  
(12)

Precision   To evaluate the precision of a probability estimator for a given policy on all the solutions simultaneously, the mean of the relative errors of the solutions is considered:

$$Err(S) = \frac{1}{\#S} \sum_{S \in S} \left| \frac{\hat{P}(S) - P_{ref}(S)}{P_{ref}(S)} \right|,$$  
(13)

where $P_{ref}(S)$ is the reference probability of the solution $S$, and $\#S$ is the cardinal of $S$.

Now, in order to compare the performance of two different policies, SPSC and MC in this article, multiple batches are executed for each policy. The previous metrics are computed for each batch and we retain in particular the mean value per policy, subsequently denoted by $Detect_{SPSC}$ and $Err_{SPSC}$ for SPSC, and $Detect_{MC}$ and $Err_{MC}$ for MC. Thus, to compare the actual gain of a policy over another, we use the following indicators:

Relative detection rate gain in %   To evaluate the gain of detection rate of SPSC over MC, the following measure is used:

$$\%Detect(S) = \frac{Detect_{SPSC}(S) - Detect_{MC}(S)}{Detect_{MC}(S)} \times 100$$  
(14)

Relative precision gain in %   To evaluate the gain of precision of estimations of SPSC over MC, the following measure is used:

$$\%Precision(S) = \frac{Err_{MC}(S) - Err_{SPSC}(S)}{Err_{MC}(S)} \times 100$$  
(15)

Relative precision gain without failure in %   To evaluate the precision of the estimation of SPSC over MC when all solutions are successfully detected, we consider the precision gain slightly modified from (15):

$$\%Precision'(S) = \frac{Err_{MC}'(S) - Err_{SPSC}'(S)}{Err_{MC}'(S)} \times 100$$  
(16)

where $Err'(S)$ represents the mean value of $Err(S)$ computed from batches that verify $Detect(S) = 1$. 
4.2 Prey-predator

We consider an agent-based prey-predator model similar to the “Wolf-Sheep” model shipped with NetLogo (Wilensky 1999) as a first example. The observables of this model are the number of living predators and preys. The following possible solutions can be considered:

- \( S_1 \): One species survives, extinction of prey and predator species, only vegetation remains.
- \( S_2 \): Two species survive, extinction of the predator species, only preys and vegetation remain.
- \( S_3 \): The three species survive and form a stable ecosystem with pseudo-periodical oscillations of their populations.

First, we run 900000 replications using MC with \( t_f = 1000 \) in order to provide reference values for the comparisons:

\[
P_{\text{ref}}(S_1) \approx 0.0065, \quad P_{\text{ref}}(S_2) \approx 0.0126, \quad P_{\text{ref}}(S_3) \approx 0.981.
\]

(17)

Then, we run 1000 batches of \( N = 50 \) replications for each policy (MC and different configurations of SPSC). The detection rate and the precision gains of SPSC over MC are shown in Figure 2.

Figure 2: Relative detection and precision gains of SPSC over MC in % for different configurations tested on the prey-predator model. The ordinate indicates the number \( m \) of sub-intervals and the abscissa represents the couple of clustering method used and number \( k \) of clusters used.
4.3 Virus

We then consider an agent-based model of virus spreading, similar to the one shipped with NetLogo as a second example. The observables of this model are the number of infected and healthy agents. The following possible solutions can be considered:

- $\mathcal{S}_1$: the virus disappears completely from the environment,
- $\mathcal{S}_2$: the virus remains in the environment.

We used the same settings as in the previous example: reference probabilities were obtained from 500000 replications with $t_f = 250$.

$$P_{ref}(\mathcal{S}_1) \approx 0.002644, \quad P_{ref}(\mathcal{S}_2) \approx 0.997356$$

Then, as previously, 1000 batches of $N = 50$ replications are executed for each policy (MC and different configurations of SPSC). The detection rate and the precision gains of SPSC over MC are shown in Figure 3.

![Figure 3](image-url)

(a) Relative detection rate gain $G_{Detect}(\mathcal{S})$ of SPSC over MC
(b) Relative precision gain $G_{Precision}$ of SPSC over MC
(c) Relative precision gain without failure $G_{Precision}'$ of SPSC over MC

Figure 3: Relative detection and precision gains of SPSC over MC in % for different configurations tested on the virus model. The axes are the same as those in Figure 2.

4.4 Microscopic traffic simulation

In this section SPSC is evaluated on a more complex use case: a microscopic traffic simulation in which agents move in the road network from an origin to a destination following a roadmap and driving rules.
An illustration of the network used in our experiments is given in Figure 4. Possible origins of vehicles are $O_1, O_2, O_3$ and $O_4$ and possible destinations are $D_1$ and $D_2$. Roadmaps are randomly generated from possible paths between origins and destinations. Agents behave according to the car-following model IDM (Treiber et al. 2000) and the French driving rules.

![Figure 4: Experimental setup for the traffic simulation. Possible origins of vehicles are $O_1, O_2, O_3$ and $O_4$ and possible destinations are $D_1$ and $D_2$.](image)

We consider, for each lane, information that allows us to determine the congestion level (i.e., mean speed and lane occupation). Therefore, the observables retrieved from a simulation state are multidimensional spatial data. Using such raw data for the partition step could lead to bad results. Thus, an autoencoder is trained beforehand on MC data in order to provide low dimensional characteristics for the partition step (Rumelhart et al. 1985; Goodfellow et al. 2016).

We assume that the local traffic state is the main indicator for the decision maker. We split the network into 3 sectors: north, center and south (corresponding respectively to red, black and blue arrows in Figure 4). We consider 2 possible traffic states within a sector: fluid, i.e. at most 2 lanes exceed experimental critical density and congested, i.e. at least 7 lanes exceed experimental critical density. Hence, we can define a set $\mathcal{S}$ of 8 solutions (2 traffic states for 3 independent sectors):

- $\mathcal{S}_1$: fluid $\times$ fluid $\times$ fluid
- $\mathcal{S}_2$: fluid $\times$ fluid $\times$ congested
- $\mathcal{S}_3$: fluid $\times$ congested $\times$ fluid
- $\mathcal{S}_4$: fluid $\times$ congested $\times$ congested
- $\mathcal{S}_5$: congested $\times$ fluid $\times$ fluid
- $\mathcal{S}_6$: congested $\times$ fluid $\times$ congested
- $\mathcal{S}_7$: congested $\times$ congested $\times$ fluid
- $\mathcal{S}_8$: congested $\times$ congested $\times$ congested

The reference values of the probability of these solutions are estimated by executing 175000 replications using MC with $t_f = 72000$:

$$
\begin{align*}
P_{\text{ref}}(\mathcal{S}_1) &\approx 0.00692 & P_{\text{ref}}(\mathcal{S}_2) &\approx 0.00023 & P_{\text{ref}}(\mathcal{S}_3) &\approx 0.0048 & P_{\text{ref}}(\mathcal{S}_4) &\approx 0.00114 \\
P_{\text{ref}}(\mathcal{S}_5) &\approx 0.00019 & P_{\text{ref}}(\mathcal{S}_6) &\approx 0.00022 & P_{\text{ref}}(\mathcal{S}_7) &\approx 0.00146 & P_{\text{ref}}(\mathcal{S}_8) &\approx 0.00437
\end{align*}
$$

Then, to compare the performances of MC and SPSC (with the number of clusters $k$ fixed to 15), 500 batches of $N = 50$ replications are executed for each policy. Since it is virtually impossible to detect all the possible solutions with only 50 replications, we modify slightly the detection metric by measuring the capability of detecting at least 2 different solutions. The detection and precision gains of SPSC over MC are shown in Figure 5.

4.5 Discussion

From the results obtained on the three examples tested here, we can conclude that in some configurations, SPSC outperforms MC in terms of the first considered metric: the detection rate (See Figures 2a, 3a, 5a).
When dealing with multiple solutions, it works extremely well with a high number of clusters \( k \). In contrast, using a small \( k \) can lead to the non-detection of some solutions. An explanation for this phenomenon is that when using a clustering algorithm with a small \( k \), some specific features of the data points could potentially be hidden if the point is assigned to a large cluster. It has to be noted that the DBSCAN algorithm, that searches automatically for potential outliers and quantifies the optimal number of clusters outperforms other clustering algorithms according to this metric.

The number \( m \) of sub-intervals seems to have an impact on the detection rate. For the prey-predator and virus models, the detection rate decreases in general while increasing \( m \). Contrarily with the transport model, the detection rate is better with high value of \( m \). A possible reason is that the prey-predator and virus models have short time interval \( t_f \leq 1000 \). Thus, replication clones might not have enough time to evolve to interesting solutions. Conversely, the time interval for the transport model is relatively large \( (t_f = 72000) \) and replication clones have enough time to evolve even with \( m = 4 \).

On the other hand, the relative errors obtained by SPSC are lower than MC in most of the cases (See Figures 2b, 3b, 5b). A tendency that can easily be observed is that bad detection rates are related to good errors and vice versa. This can be explained by the fact that the value of the reference probability is very small, which leads to a paradoxical situation: the non-detection of such a solution (the probability is estimated by 0 in this case) results in a very small relative error. However, when considering the precision gain without failure (i.e., when the execution policy did not fail to detect the solution), it is clear that SPSC allows one to obtain better estimates (See Figures 2c, 3c, 5c). Once again, DBSCAN turns to be one of the best clustering algorithms among those tested in these experiments.

5 CONCLUSIONS AND PERSPECTIVES

We have presented in this paper an execution policy named SPSC which can be more efficient than MC with limited resources. Contrary to existing specialized methods discussed in Section 2.3, SPSC is generic and easy to apply, since the simulations are treated as black boxes and no specific information about the possible solutions is needed. The only operational constraint imposed by SPSC on the simulation environment is the ability to clone replications.

Some configurations (using different partitioning algorithms and \( k \)) of SPSC were tested with three different stochastic multi-agent-based simulations. The results comparison shows that, using the appropriate configuration, SPSC detects the possible solutions and estimate their probabilities better than MC, especially when the clustering algorithm DBSCAN is used for the partition step. On the other hand, in this study,
replications were cloned with the same rate. Investigating the impact of different cloning policies on the quality of the results would be interesting.

The microscopic traffic simulation presented in Section 4.4 was based on a simple network topology. From an experimental point of view, our main perspective is to validate SPSC on a realistic multi-modal network at the city scale. From a more theoretical point of view, an extension of SPSC, using modern statistical inference tools (e.g., based on belief functions (Kanjanatarakul et al. 2016)) and probabilistic clustering algorithms (Ross 2010) can be envisaged as we deal with small samples at each intermediate time step.

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