

DISCRETE UNIVARIATE RANDOM VARIATE GENERATION

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Most of the early research done in random variate generation is in the area of continuous distributions. Not until 1979 was research published on exact, uniformly fast discrete univariate random variate generation. Since then the state of the art of discrete univariate random variate generation has been advanced steadily, and exact, uniformly fast algorithms are now available for Poisson, binomial, hypergeometric and negative binomial distributions. This paper surveys the algorithms for these commonly used univariate discrete distributions. Timing comparisons of some of the algorithms are presented along with the references of recent papers. A copy of the visual aids is also given.

BIBLIOGRAPHY

- Ahrens JH, Dieter U (1974), Computer Methods for Sampling from Gamma, Beta, Poisson and Binomial Distributions, Computing, Vol. 12, pp. 233-246.
- Ahrens JH, Dieter U (1980a), Sampling from Binomial and Poisson Distributions: A Method with Bounded Computation Times, Computing, Vol. 25, pp. 193-208.
- Ahrens JH, Dieter U (1982), Computer Generation of Poisson Deviates from Modified Normal Distributions, ACM Transactions on Mathematical Software, Vol. 8, No. 2, pp. 163-179.
- Atkinson AC (1979), The Computer Generation of Poisson Random Variables, Applied Statistics, Vol. 28, No. 1, pp. 29-35.
- Chen HC, Asau Y (1974), On Generating Random Variates from an Empirical Distribution, AIEE Transactions, Vol. 6, pp. 163-166.
- Devroye L (1980a), The Computer Generation of Poisson Random Variables, Technical Report, McGill University, Canada.
- Devroye L (1980b), The Computer Generation of Binomial Random Variables, Technical Report, McGill University, Canada.
- Devroye L (1980c), Generating the Maximum of Independent Identically Distributed Random Variables, In: Computers and Mathematics with Applications.
- Devroye L, Naderisamani A (1980), A Binomial Random Variate Generator, Technical Report, McGill University, Canada.
- Fishman GS (1973), Concepts and Methods in Discrete Event Digital Simulation, John Wiley and Sons, New York.
- Fishman GS (1976), Sampling from the Poisson Distribution on a Computer, Computing, Vol. 17, pp. 147-156.
- Fishman GS (1978), Principles of Discrete Event Simulation, John Wiley and Sons, New York.
- Fishman GS (1979) Sampling from the Binomial Distribution on a Computer, Journal of the American Statistical Association, Vol. 74, No. 366, pp. 418-423.
- Fishman GS, Moore LR (1982), Sampling From a Discrete Distribution while Preserving Monotonicity, Technical Report No. UNC/ORSA/TR-81/7, Curriculum in Operations Research and Systems Analysis, University of North Carolina at Chapel Hill.
- Kachitvichyanukul V, Schmeiser BW (1983a), Binomial Random Variates Generation, Technical Report, Purdue University, West Lafayette, IN.
- Kachitvichyanukul V, Schmeiser BW (1983b), Computer Generation of Hypergeometric Random Variate, Technical Report 83-1, Program in Industrial and Management Engineering, The University of Iowa, Iowa City, Iowa, 52242.

- Kronmal RA, Peterson AV Jr (1979a), On the Alias Method for Generating Random Variables from a Discrete Distribution, American Statistician, Vol. 33, No. 4, pp. 214-218.
- Kronmal RA, Peterson AV Jr (1979b), The Alias and Alias-Rejection-Mixture Methods for Generating Random Variables from Probability Distributions, In: 1979 Winter Simulation Conference, H.J. Highland, M.G. Spiegel, R. Shannon (eds.), IEEE, pp. 268-280.
- Kronmal RA, Peterson AV Jr (1981), A Variant of the Acceptance-Rejection Method for Computer Generation of Random Variables, Journal of the American Statistical Association, Vol. 76, No. 374, pp. 446-451.
- Léger R (1973), On sampling from the negative binomial and Weibull distributions, Master's thesis, Dalhousie University, Halifax, N.S.
- Lewis PAW, Shedler GS (1979), Simulation of Nonhomogeneous Poisson Processes by Thinning, Naval Research Logistics Quarterly, Vol. 26, No. 3, pp. 403-413.
- Marsaglia G (1963), Generating Discrete Random Variables in a Computer, Communications of the ACM, Vol. 6, pp. 37-38.
- McGrath EJ, Irving DC (1973), Techniques for Efficient Monte Carlo Simulation: Volume II; Random Number Generation for Selected Probability Distributions, National Technical Information Service, U.S. Department of Commerce.
- Norman JE, Cannon LE (1973), A Computer Program for the Generation of Random Variables from any Discrete Distribution, Journal of Statistical Computation and Simulation, Vol. 1, pp. 331-348.
- Pak CH (1975), The Generation of Poisson Random Variables, Journal of the Korean Institute of Industrial Engineering, Vol. 1, No. 1, pp. 87-92.
- Relles DA (1972), A Simple Algorithm for Generating Binomial Random Variables When N is Large, Journal of the American Statistical Association, Vol. 67, pp. 612-613.
- Schmeiser BW (1980), Random Variate Generation: A Survey, In: Simulation with Discrete Models: A State of the Art View, T.I. Oren, C.M. Shub, P.F. Roth (eds.), Winter Simulation Conference, IEEE, pp. 79-104.
- Schmeiser BW (1981), Random Variate Generation, In: 1981 Winter Simulation Conference Proceedings, T.I. Oren, C.M. Delfossé, C.M. Shub (eds.), IEEE, pp. 227-242.
- Schmeiser BW, Kachitvichyanukul V (1981), Poisson Random Variate Generation, Technical Report, Purdue University, West Lafayette, IN.
- Snow RH (1968), Algorithm 342: Generator of Random Numbers Satisfying the Poisson Distribution, Communications of the ACM, Vol. 11, No. 12, pp. 819-820.
- Tadikamalla PR (1979), A Simple Method for Sampling from the Poisson Distribution, Working paper 365, Graduate School of Business, University of Pittsburgh.
- Tocher KD (1963), The Art of Simulation, D. Van Nostrand Company, Princeton, New Jersey.
- Walker AJ (1977), An Efficient Method for Generating Discrete Random Variables with General Distributions, ACM Transactions on Mathematical Software, Vol. 3, pp. 253-256.