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A PROTOTYPE IMPLEMENTATION OF AN EMBEDDED SIMULATION SYSTEM FOR THE STUDY OF LARGE SCALE ICE SHEETS

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ABSTRACT

Understanding the impact of global climate change on the world's ecosystem is critical to society at large and represents a significant challenge to researchers in the climate community. One important piece of the climate puzzle is how the dynamics of large-scale ice sheets, such as those covering Greenland and Antarctica, will respond to a warming climate. Relatively recently, glaciologists have identified ice streams, which are corridors of ice that are flowing at a much higher rate than the surrounding ice, as being crucial to the overall dynamics and stability of the entire ice sheet. However, ice stream dynamics, and their impact on the entire ice sheet, are far from understood. It is thus critical to develop simulation models through which these important issues can be studied. In this paper, we present one novel approach to developing such simulation capabilities through the use of *embedded simulation*.

1 INTRODUCTION

Ice streams are fast-moving corridors of ice that originate in the interior of an ice sheet and drain into the sea through what are termed *outlet glaciers*. They have very different dynamics than the rest of the ice sheet, and need to be modeled at a much higher resolution to develop better insight into their behavior and impact on overall ice sheet dynamics. This represents a significant challenge for ice sheet modelers, because even small increases in resolution often result in tremendous increases in both computational costs and the sizes of the input/output data sets that must be handled by the simulation. For example, modeling the Greenland ice sheet at a resolution of 5-km requires on the order of 34 million grid points and data sets on the order of 1-GB. Increasing to the 1-km resolution, however, increases the number of grid points to over 1.6 billion, and increases the size of the data sets to over 28GB. Modeling at a resolution of 500 meters, which appears to be a minimum resolution for the study of ice streams, would increase the number of grid points in the simulation from 1.6 billion to over 6.7 billion. It would similarly increase the size of the input/output files to over 125GB. While these file sizes may be manageable if output is only written to disk at the end of the run, it is often the case that they need be saved on a much more frequent basis, such as when creating animations of ice sheet dynamics over time and when performing basic state saving for error recovery.

Given these difficult challenges, we are pursuing a different technique using *embedded simulation*. In this approach, areas of the ice sheet undergoing rapid change are modeled at the highest resolution available, while the interior portions of the ice sheet, whose dynamics are evolving much less rapidly, are modeled at lower resolutions. In fact, we believe it is somewhat more intuitive to view this modeling

problem in terms of multiple physical processes, executing at different spatial and temporal resolutions, each of which can interact with and impact the behavior of the other physical processes. In this paper, we present our approach that provides the synchronization and communication mechanisms that enable such simulation modeling.

We are developing our approach using the Parallel Ice Sheet Model (PISM), which is a widely used parallel simulation model for the study of large-scale ice sheets (Torsten Albrecht, et. al, 2015). It involves implementing multiple, independent instances of a full PISM simulation, one for each region of the ice sheet being simulated at different resolutions. We then add the communication and synchronization mechanisms necessary to correctly capture the important feedback loops between these models and to maintain the fidelity of the overall ice sheet simulation.

We believe this paper provides two important contributions to the modeling and simulation community. First, it provides a clear proof of concept for this basic approach. This is demonstrated through experimental results that document the accuracy of the overall simulation, and that provide strong indications that it is able to capture important feedback loops between the simulation processes.

Second, while the focus of this paper is on large-scale ice sheet modeling, we believe the basic approach will have much broader applicability. In particular, large scientific modeling applications, where the domain is laid out across a checkerboard grid and includes processes logically executing at different special and temporal resolutions, could derive significant benefits from using this approach.

The rest of the paper is organized as follows. In Section 2, we provide an overview of PISM and its approach to modeling ice dynamics. In Section 3, we describe our approach to the development of embedded simulation modeling. In Section 4, we discuss our experimental design, and we provide our experimental results in Section 5. We discuss related research in Section 6, and provide our conclusions and future research in Section 7.

2 THE PARALLEL ICE SHEET MODEL (PISM)

PISM is a powerful and highly flexible parallel simulation model that provides researchers with a window into past, present, and future behavior of large-scale ice sheets. It provides multiple algorithms for modeling ice sheet dynamics and how such dynamics change over time. This includes the Shallow Ice Approximation (Le Meur et al. 2004), the Shallow Shelf Approximation (Bueler and Brown, 2004), and a hybrid 'SSA + SIA' model (Winkelmann et al. 2011) for the solution of stress balance equations. It provides ways to customize and combine such models to fit the problem at hand, and makes available a wide range of models for marine ice physics, ocean calving, and conservation of energy. PISM also provides the ability to easily couple the simulation with external ocean and atmospheric models.

Within PISM, the model takes place in a rectangular computational box that consists of a collection of data points in three dimensions representing the space that encloses the glacier being studied. In each of the x and y dimensions, the grid points are equally spaced, and have a relatively coarse resolution. The z dimension is given a relatively finer resolution than x or y, and the spacing of grid points along this dimension may vary within a given model allowing for more detail near the base of the ice where driving forces are greatest. Each x, y pair represents a single column of ice that is parallel with the force of gravity.

PISM takes the entire computational box and divides it into n rectangular sub-grids, where n is the number of processes being used for the simulation. It attempts to make the sub-grids as square as possible in the x and y dimensions because the calculation of a new value for a given grid point often only depends on the current values of variables at adjacent grid points. Therefore, the degree to which the computation of one sub-grid depends on results from another sub-grid is proportional to the perimeter of the local grid, and the square has the minimum perimeter for any rectangle. However, for many computational box sizes and values of n, there is no way to evenly distribute the grid points to n non-intersecting squares. In such cases, PISM arranges the sub-grids into r rows and c columns with $n = rc$, with no row being more than

one grid point wider than any other row, and no column being more than one grid point taller than any other column.

PISM is an iterative, numerical simulation that progresses in units of *time steps*. At the beginning of each time step, the simulation components cooperatively determine the amount of *logical time* by which the simulation can be advanced while preserving the basic numerical and physical consistency constraints of the underlying physics being modeled. This amount of logical time can be thought of in much the same way as the *look-ahead* value in a conservative, parallel discrete event simulation. Once the duration of the time step has been determined, PISM utilizes an interpolation process (between neighboring grid points) to determine the *initial,* or *boundary conditions* for the current step. It then models the evolution of ice dynamics over the period of logical time determined at the beginning of the time step. This process is repeated until the simulation is completed.

PISM derives its computational scalability from its use of the Portable Extensible Toolkit for Scientific Computation (PETSc, Satish et al., 2015, 2015a, 1997), which is a widely used library of data structures and routines for scientific models that require partial differential equations for their solutions. PETSc, in turn, derives its scalability by spreading its computation across multiple processing cores and using MPI (The Message Passing Interface Standard) for inter-process communication.

3 APPROACH

In this prototype implementation, we use a simulation of the whole Greenland ice sheet executing at a resolution of two kilometers, within which we embed a 500-meter resolution simulation of the Jakoshabvn outlet glacier, which is located on the western coast of Greenland. We chose this particular outlet glacier for three reasons. First, it is the fastest flowing glacier in the world (Moulins, 2008), through which approximately 7% of the entire ice sheet is discharged into the ocean (Torsten Albrecht, et. al, 2015). Second, this area experienced a significant calving event quite recently in 2015, and has retreated over 35-km in the last 150 years. Third, we have 500-meter resolution data sets for this region of the ice sheet, provided by the Center for Remote Sensing of Ice Sheets (CReSIS, https://www.cresis.ku.edu/), which are available at (https://data.cresis.ku.edu/data/).

The high- and low-resolution simulations are implemented as two independent instantiations of a PISM model, each of which is fully parallelized and, in isolation, correctly synchronized by its respective runtime system. However, they share an overlapping region of the grid in which one simulation can *directly* impact the model state of the other, requiring careful synchronization to correctly capture their interactions while maintaining coherence of the overall simulation.

The overlapping region of the ice sheet is partially depicted in Figure 1. It is important to note that the high-resolution grid points are fully contained within the embedded region, while the low-resolution grid points cover the entire domain (ice sheet), *including* the embedded region.

3.1 Boundary Conditions

Recall that PISM computes new boundary conditions at the beginning of each time step through the application of an interpolation algorithm applied to each grid point and its nearest neighbors. We use a similar approach in the computation of the boundary conditions at the beginning of a new time step for both the high- and low-resolution simulations. In fact, it is the computation of such initial boundary conditions that largely captures the interactions between the two simulations.

First, consider the embedded simulation. Initial boundary conditions are computed for the high-resolution grid points lying at the *border* of the embedded region at the beginning of a time step. For each such point, the four nearest low-resolution grid points (termed *neighbors*) are determined. The initial values of these points are then computed using a *weighted linear interpolation* of the values from the chosen low-resolution neighbors. Thus while several high-resolution grid points may share the same set of low-resolution neighbors, the impact of each neighbor is weighted by its relative distance from the high-resolution point under consideration. This process is depicted in Figure 2.

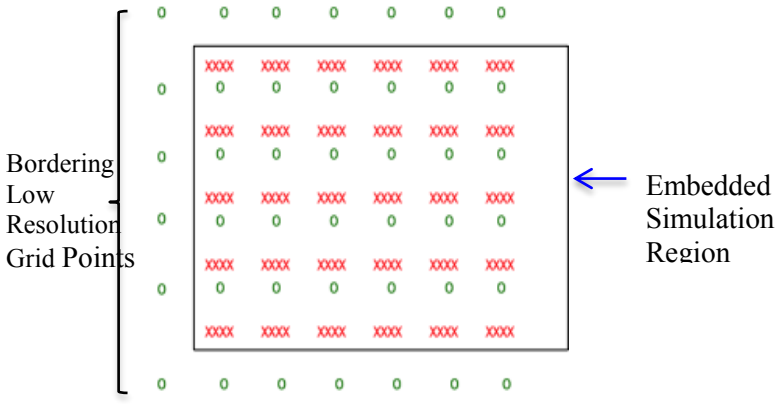

Figure 1: This figure depicts the distribution of high- and low-resolution grid points within the high-resolution embedded region of the grid. The high-resolution grid points are depicted as 'x', and the low-resolution grid points are depicted as 'o'. Note that we show only the low-resolution grid points within and immediately surrounding the embedded region.

As noted above, the state of the high-resolution simulation is impacted by the low-resolution simulation through the computation of the initial boundary conditions at each new time step. This impact is propagated throughout the high-resolution domain by PISM's subsequent modeling of the evolution of ice dynamics throughout the subsequent time step. The impact of the high-resolution simulation on the state of the low-resolution simulation is captured in a similar manner. In particular, each low-resolution point within the embedded region determines it's closest four neighboring high-resolution grid points, and computes its boundary conditions using a weighted linear interpolation of these neighbors. The impact of the new boundary conditions is then propagated throughout the low-resolution model in the subsequent time step.

3.2 Two Phase Synchronization Protocol

Assume the simulations are synchronized at some logical time **T1** representing the beginning of a new time step. At this point, the newly computed values of the low-resolution grid points within the embedded region are communicated to the low-resolution simulation. These new grid points are then placed into the embedded region of the ice sheet. From this point forward, the time step is controlled by PISM. It utilizes the modified values from the high-resolution simulation in the computation of the initial conditions, and then executes the simulation to the end of the time step, call it logical time **T2**, using its normal processes. Once the simulation reaches logical time **T2**, it sends to the high-resolution simulation the newly computed values of grid points bordering the embedded region of the ice sheet. It then blocks, waiting for the high-resolution simulation to execute up to logical time **T2**. This represents the end of Phase 1 of the protocol.

In Phase 2 of the protocol, the high-resolution simulation is executed from logical time **T1** to **T2**. However, because it is being modeled at a higher resolution, it typically takes several, much smaller time steps, to model its evolution over this same time interval. Ideally, we would like to use the values of the bordering grid points (from the low-resolution model) in the computation of the boundary conditions for each of these smaller time steps, but such information is only available for logical times **T1** and **T2**. We therefore use a linear 2D interpolation between the values provided for logical times **T1** and **T2** in the computation of subsequent boundary conditions. Once the high-resolution simulation reaches logical time **T2**, it provides to the low-resolution simulation the updated values of the grid points within the embedded region. This process continues to the end of the simulation.

To summarize, the interactions between the simulation models are captured through the values of the grid points that are exchanged and utilized in the computation of initial boundary conditions. The impact

of such interactions on the evolution of ice dynamics is propagated throughout the respective simulations via the subsequent execution of the PISM model.

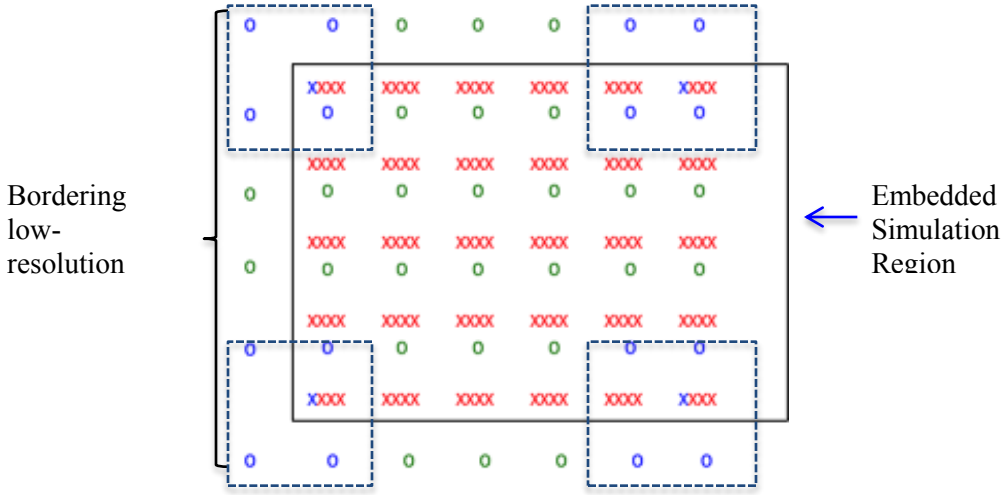

Figure 2: This figure partially depicts the process of establishing initial boundary conditions for the high-resolution grid points. The high-resolution points are depicted as 'x', and the low-resolution grid points are depicted as 'o'. For each high-resolution grid point along the border of the embedded region the four closest low-resolution points are selected. The initial boundary conditions are then established utilizing a weighted linear interpolation between these neighbors. For example, consider the four high-resolution points represented as 'x'. The figure shows the corresponding low-resolution grid points that will be used for the interpolation (represented as 'o').

4 EXPERIMENTAL DESIGN

All of our experimental results were obtained utilizing the SuperMic cluster located at the High Performance Computing Center at Louisiana State University. It consists of 360 compute nodes, each of which includes two 10-core Intel Xeon Ivy Bridge-EP E5-2680 processors operating at a rate of 2.8 GHz. Each node also provides two Intel Xeon Phi 7120P coprocessors that have not yet been incorporated into our initial implementation. Each node is equipped with 64GB DDR3 1866MHz Ram, and a 500GB hard drive. It is attached to the rest of the system via a 56 Gigabit per second Infiniband network interface. Each node runs the Red Hat Enterprise 6 operating System.

We tested our prototype implementation using a 2-km model of the entire Greenland ice sheet with an embedded model of the Jakobshavn outlet glacier region at a 500-meter resolution. Our primary goal was to provide a proof of concept for the basic approach we are pursuing. To help determine the validity of our approach, we wanted to compare ice velocities computed by our simulation with those obtained through direct observation and measurement. We also wanted to demonstrate the impact of model resolution on simulation results in this critical domain. Finally, we wanted to establish baseline performance metrics to gauge the impact of various optimization techniques under development.

5 EXPERIMENTAL RESULTS

We first compare the ice velocities computed by our simulation with those obtained from direct observation and measurement (Joughin et. al, 2010). The computed and observed velocities were taken from a 10-km cross-section of the ice flow within the Jakobshavn outlet glacier. The measurements were taken between the grounding line, where ice begins to float, and the Calving Front, which is where floating ice detaches from the ice sheet. The results are shown in Figure 3.

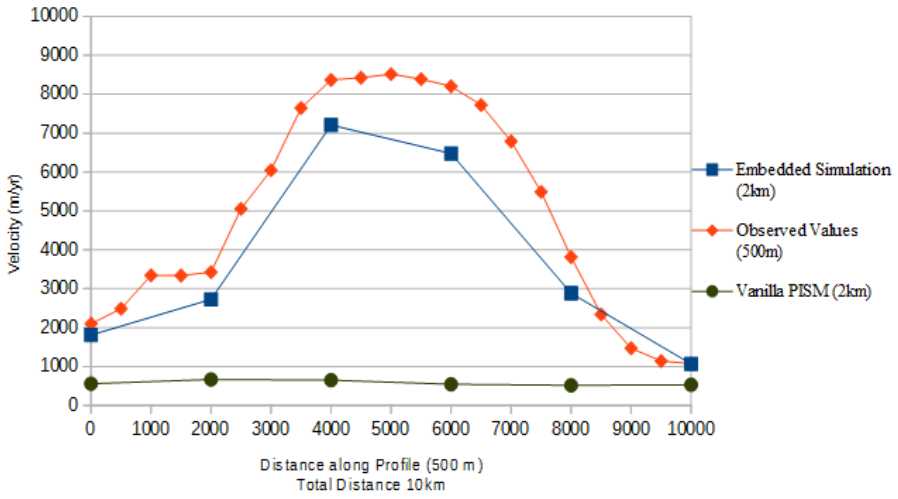

Figure 3: This graph shows the observed ice velocities (top), the simulated velocities using the embedded simulation (middle), and the velocities computed by the non-embedded simulation.

The top line in the graph represents the observed ice velocities sampled at 500-meter resolution. The next line shows the values of the *low-resolution grid points* that fell within the embedded region. For comparison purposes, we also included the simulated velocities computed by a 2-km non-embedded simulation.

As can be seen, the velocities computed using embedded simulation are reasonably close to the observed values, and even begin to capture the basic shape of the curve of observed values toward the middle of the cross section. It is very interesting to note that the results clearly demonstrate a feedback loop between the high- and low-resolution simulations operating within the embedded region of the grid. This can be seen by comparing the results provided by the embedded simulation, which represent the values of the low-resolution grid points within the embedded region, to the third set of results, which represent the same grid points as computed by the 2-km whole ice sheet model. The differences in these velocities are directly attributable to the impact of the high-resolution simulation on the values of the low-resolution grid points.

5.1.1 Computational Costs

We also wanted to provide a baseline measure of the computational costs incurred by the prototype implementation of our system. We measured this by executing both a non-embedded, 2-km simulation of the whole Greenland ice sheet and the same model with the embedded simulation. We executed both models for one logical year. The results are provided in Table 1.

Table 1: This table provides basic performance characteristics of our prototype embedded simulation system.

Performance Metrics	**2KM Vanilla**	**2KM with 500-meter embedded**
Number of processors	700	350 per model
Total Run time	300.44s	6373.20s
Total Wait time	0s	1037.90s
Total Number of time steps	277	8694

The most striking result is the fact that it took approximately 21 times as long to execute the 2-km embedded simulation model as it did to execute the non-embedded model. There are several contributing factors leading to the increased computational costs. One such factor is a 31-fold increase in the number of time steps required to complete the simulation. And while an increase in the number of time steps was certainly expected, the magnitude of the increase was somewhat surprising. However, this is a cost that will be incurred by any simulation model using a time stepping algorithm to resolve dynamic processes at high resolution.

The other contributing factors are largely related to the initial implementation techniques. One problem is that the system does not yet support processor sharing between simulations, and, in this example, simply divided the total number of available cores equally between them. Because of the blocking nature of the simulation protocol, this led to lengthy wait times during which one half of the computational resources were idle. We discuss our strategies for addressing these issues in Section 7.

6 RELATED WORK

The PISM developers are also investigating solutions to these same challenges. One approach that has been implemented within PISM is the ability to perform *regional* simulation models at high resolutions (Torsten Albrecht, et. al, 2015). Similar to the ideas outlined in this paper, their goal is to only simulate at high resolution in regions of the ice sheet undergoing rapid change. However, in their approach the high-resolution simulation executes in isolation, and there is no mechanism to feedback results from the high-resolution region of the grid to other regions of the ice sheet.

A recently published paper (Aschwanden, 2016), describes a whole Greenland ice sheet model, executing at a constant 600-meter resolution, which is implemented within PISM. The model was executed out 100 years, and produced simulated ice velocities, for a number of outlet glaciers across Greenland, which fit observed values quite well. Unfortunately, the computational costs of their approach, including the costs of performing I/O at such high resolutions, were not discussed in the paper. We are working on obtaining such results, but were unable to do so by the time of this writing.

Other available parallel ice sheet models with higher-order capability include the Ice Sheet System Model (ISSM, (Larour et al. 2012)), and we have pursued incorporating CReSIS high-resolution bed-maps into this model. One advantage of ISSM is its ability to generate and use a variable-resolution grid. ISSM provides interpolation tools that take regular checkerboard grids (rows and columns, uniformly spaced and aligned with the coordinate axes) such as those provided by CReSIS, and based on some external metric (usually measured velocity if available, although it can be specified manually), provide non-uniform triangular element grids that provide higher resolution where needed, and lower resolution where it is not. Similar to the paper describing the 600-meter whole ice sheet model, we have been unable to find detailed discussions of the computational costs of the ISSM approach.

While we have thus far discussed our research in terms of numerical simulation modeling, the approach we are pursuing begins to incorporate some of the basic synchronization techniques and ideas found within the parallel discrete-event simulation community. Viewed in this way, our approach is essentially an enhanced window-based synchronization protocol quite similar to the YAWNS protocol

(Nicol, 1993). Given the high blocking costs incurred by our two-phase synchronization protocol, it becomes attractive to think in terms of integrating optimistic synchronization techniques, e.g., Bounded Time Warp (Turner and Xu,, 1992), into our embedded simulation system.

7 CONCLUSIONS AND FURTURE RESEARCH

In this paper, we have presented our design and prototype implementation of a high-resolution simulation for regions of an ice sheet undergoing rapid change, embedded within a lower-resolution model for regions of the ice sheet that are evolving at a much slower rate. We have described our approach to integrating the results from simulations that are operating at different spatial and temporal resolutions, while maintaining the coherence of the overall system. We demonstrated one important feedback loop within the shared region of the grid, and showed that the computed ice velocities compare quite well, although not yet perfectly, to the observed values. We believe that other, larger feedback loops will also be captured with extended simulation runs. Overall, we are pleased with the success of the prototype.

There is of course much work remaining, the most important of which is reducing the computational costs of the prototype implementation. There are three basic approaches under investigation. First, we are conducting very basic load-balancing experiments to determine the number of cores to allocate to each simulation to minimize the wait time. Second, we are in the process of incorporating the two Intel Xeon Phi 7120P coprocessors into the system. This would serve to provide additional (free) computational resources as well as more extensive opportunities for load balancing. Third, we are interested in implementing gang scheduling such that both simulations utilize the same set of computational resources. This would largely eliminate blocking, but this would come at the expense of increased context switching costs.

We are also interested in embedding multiple high-resolution simulations within a low-resolution whole ice sheet model. We believe this will represent a straightforward extension of the current approach, and could provide a much deeper understanding of underlying physical processes being modeled.

Our longer-term goal is to utilize optimistic simulation techniques to further reduce cost of blocking that is inherent in conservative simulation approaches. However, more research is needed to determine the opportunities for optimistic execution, and to define the error conditions that would require rolling back to an earlier state.

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